

CS 151
Final Exam
Fall 2021

Name _____

Unless you qualify for extended time on exams, **you have 2 hours to complete this exam** once you start it.

The 8 numbered questions are equally weighted.

If you forget the name of something (oh, what does Java call the length of a String??) just write a note saying "I'm going to call this X" and then use that.

Please do not write on the backs of the pages. If you need more space for a question there are two blank pages at the end.

After you have finished the exam please indicate whether you followed the Honor Code on the exam.

I ☐ did ☐ did not

adhere to the Honor Code while taking this exam.

I started the exam at time _____ and finished at time _____

Signature

1. Here is a list of data: 11 4 15 7 3 14 2 10. For each of the following structures I will walk through the data list in order, add each item to the structure and then go into a loop in which I remove elements one at a time from the structure and print them as I remove them. **In what order do I print the items for**
- a) **A stack.** Using `push()` to add to the structure and `pop()` to remove.
 - b) **A queue.** Using `offer()` to add to the structure and `poll()` to remove.
 - c) **A priority queue.** Using `offer()` to add to the structure and `poll()` to remove.
 - d) In the add stage, I insert the values into a **BinarySearchTree** that starts off empty. So 11 becomes the root and I insert the other values around it. Skip the remove stage and instead give an **inorder traversal** of the tree.
 - e) This is the same as (E) only I do a **preorder traversal** of the tree.
 - f) **In the add stage I form a hash table of size 8** (the data fits; you don't need to resize the table) with linear open addressing, using each data value as its own hash code (so the **hash value is the remainder when we divide the value by 8 -- 4 hashes to index 4, 11 to index 3, 15 to index 7, etc.**) In the print stage I print the data at index 0, then the data at index 1, then index 2, etc.

2. In each part **give a Big-Oh estimate of the worst-case time it takes to complete the operation in the given structure**

- a) Inserting into an AVL tree with n nodes

- b) Finding, then removing, a node from a Binary Search tree

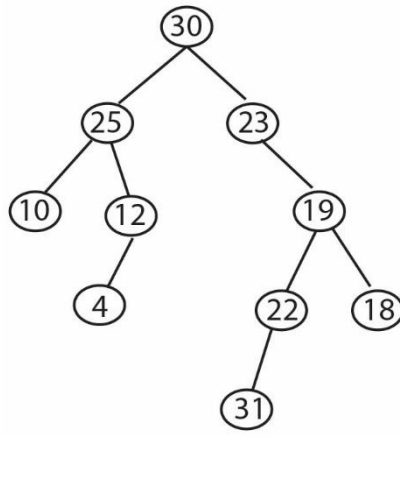
- c) Finding an element in a sorted ArrayList with n elements. Here “finding” means determining if the list contains an element with a particular value.

- d) Finding an element in a sorted LinkedList with n elements.

- e) Polling a Priority Queue with n values.

- f) Inserting an Edge in the graph structure we used in Lab 9, if there are n vertices in the graph and we are given the names of the source and destination nodes of the edge. For this one give the average-case time rather than worst-case time.

3. Here is a binary tree based on the following Node type:
- ```
class Node {
 int data;
 Node leftChild;
 Node rightChild;
}
```

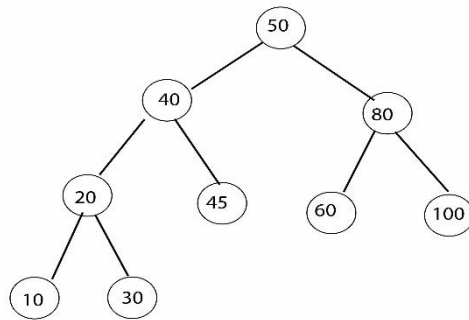


A breadth-first traversal of a binary tree lists the root, then the root's children, then their children, and so forth. A breadth-first traversal of the example tree is

30 25 23 10 12 19 4 22 18 31

Write the method **void PrintBreadthFirst( Node root )** which prints a breadth-first traversal of the tree with the given root.

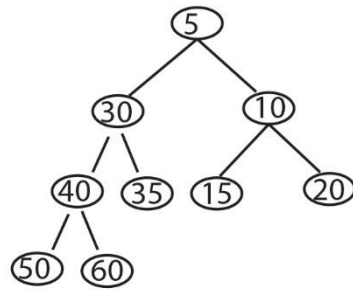
4. Here is an AVL tree:



**Give either the AVL tree or a level-by-level listing of the AVL tree that results from inserting value 25 into this tree.** If you can't easily draw a tree, a "level-by-level listing" of a tree lists the root on the first level, all of the children of the root on the second level, the grandchildren of the root on the third level, and so forth. A level-by-level listing of the tree shown is

50  
40 80  
20 45 60 100  
10 30

5. Here is a picture of a binary Heap represented as a tree:



If you prefer this could be represented as an array:

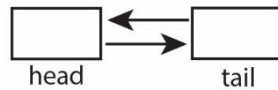
|  |   |    |    |    |    |    |    |    |    |
|--|---|----|----|----|----|----|----|----|----|
|  | 5 | 30 | 10 | 40 | 35 | 15 | 20 | 50 | 60 |
|--|---|----|----|----|----|----|----|----|----|

**Give the heap (either the array or the tree) that results from polling the heap to remove the root value 5.**

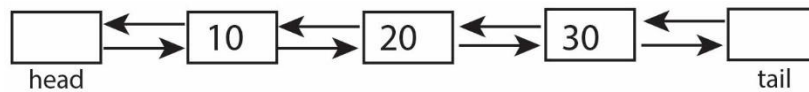
6. We have a doubly-linked list based on the following node structure:

```
class Node {
 int data;
 Node next;
 Node previous;
}
```

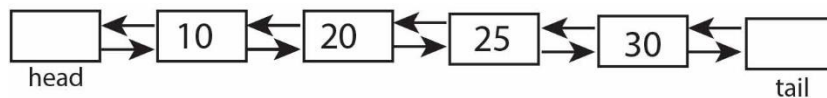
Our list has sentinel nodes with no data at each end. Here is the empty list created by the list constructor:



Here is a list with three elements:



**Give code for the method `void InsertInOrder(int v)`.** If the list is sorted this inserts `v` in the proper location for it to remain sorted; if the list is not sorted when this is called it can insert `v` anywhere. If we call `InsertInOrder(25)` with the 3-element example above it produces



7. In Lab 3 we solved mazes. A maze in that lab was a rectangular grid of Squares, where a Square could be the maze's entrance, its exit, a wall, or an open space. A solution was a path of open squares connecting the entrance to the exit. We wrote two programs to solve mazes: MazeSolverStack and MazeSolverQueue. They both worked but you have learned so much since then. Give an algorithm in English for finding the *shortest* path from the entrance to the exit of a maze.

8. Suppose you have a `Queue<E>` implementation and you need to add the following method to it: `boolean MoveToFront(E elt)`. If object `elt` is in the queue this method removes the first instance of it from the queue, moves it to the head of the queue (so it will be the next thing returned by `poll()`) and returns `true`. If `elt` is not in the queue `MoveToFront(elt)` doesn't change the queue at all but returns `false`. Give an algorithm in English for `MoveToFront()`. You can use any data structures you want but you cannot make any assumptions about the underlying structure of `Queue<E>`.

You can use this page as extra space for any question. Be clear about which question you are answering.

And here is even more extra space.