

Scalable Decision-Theoretic Planning in Open and Typed Multiagent Systems

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Problem: Scalable Planning in Open Environments

Many-Agent Environments: environments with dozens to thousands of agents

Open Environments: agents join and leave the environment (temporarily or permanently) over time

- Real-world Examples:** wildfire fighting, autonomous ridesharing, cybersecurity
- Problem:** Openness requires agents to not only predict what actions their peers will take in order to choose a best response, but also *first estimate which peers will even be present to take actions*



- Tracking the presence of neighbors results in a *more complicated problem model*. The increase in the problem model size is:

- exponential* if agent presence is considered in the environment state, which is intractable, especially for many-agent environments
- only *linear* if agent presence is considered within the mental models of each agent in an I-POMDP-Lite problem model (or other I-POMDP variants)

- Larger planning problem *affects scalability* as the number of agents increases (to many-agents)
 - MCTS algorithms: each trajectory requires sampling actions for all neighbors, so more agents results in fewer sampled trajectories in a fixed time budget (for responsive reasoning)
 - With openness, time is also spent updating estimates of presence of each neighbor, further reducing the number of trajectories possible within a time budget
 - Frame-action Anonymity** offers some relief by replacing joint actions with counts of actions called **configurations** C when environment dynamics *do not depend on which agents* take which actions.
 - Key observation:** estimating *counts* of actions might not require estimating actions for all agents *individually*

Solution: Many-Agent Planning under Openness



Main principle: *only model some neighbors* to counter the increased complexity caused by openness

- In polling and survey theory, social scientists only survey a small randomly sampled portion of the population to estimate the behaviors and opinions of all people

Subject agent estimates action counts for the entire neighborhood by *extrapolating* the estimated actions of modeled neighbors $\hat{N}_\theta(i)$ using the **multinomial distribution**

$$P(C_\theta | s^t, M^t) \sim \text{Multi}(|N_\theta(i)|, \{\hat{p}_{a_1, \hat{N}_\theta(i)}, \dots, \hat{p}_{a_{|A|}, \hat{N}_\theta(i)}\})$$

$$\hat{p}_{a, \hat{N}_\theta(i)} = \frac{\hat{n}_{\pi(s^t)=a, \hat{N}_\theta(i)}}{|\hat{N}_\theta(i)|}$$

I-POMCP_O Many-Agent MCTS Algorithm: adapts POMCP algorithm to many-agent open environments

- Estimate actions of a few neighbors then extrapolate to all neighbors' behaviors
- Better time complexity** than previous I-POMCP MCTS algorithm (Hua et al., 2015).
- Comparable to Dec-POMDP MCTS algorithms (Amato & Oliehoeck, 2015; Best et al., 2019) *but does not require* the subject agent to observe other agents' actions nor their observations

Algorithm 1 I-POMCP_O: Open Many-Agent MCTS

Note: T is the tree (initially empty), p is a path from the root of the tree (with $p = \emptyset$ signifying the root), B_p is the particle filter signifying the set of state-model pairs encountered at the node at p in the tree, PF is the root particle filter, N is count of the number of visits to each node in the tree initialized to some constant $\nu \geq 0$, Q is the Q function initialized to 0, c a constant from UCB-1.

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1: procedure I-POMDP-MCTS( $PF, \tau$ )
2:    $time \leftarrow 0$ 
3:   while  $time < \tau$  do
4:      $s^0, M^0 \leftarrow \text{SampleParticle}(PF)$ 
5:      $\text{UpdateTree}(s^0, M^0, 0, \emptyset)$ 
6:      $Increment\ time$ 
7:      $return\ \text{argmax}_{a \in A_i} Q(\emptyset, a)$ 

1: procedure  $\text{UPDATETREE}(s^t, M^t, t, p)$ 
2:   if  $t \geq H$  then
3:      $return\ 0$ 
4:    $B_p \leftarrow B_p \cup \{(s^t, M^t)\}$ 
5:   if  $p \notin T$  then
6:      $T \leftarrow T + \text{leafnode}(p)$ 
7:      $return\ \text{Rollout}(s^t, M^t, t)$ 
8:   else
9:      $C^t \leftarrow \text{SampleConfiguration}(s^t, M^t)$ 
10:     $a_i^t \leftarrow \text{argmax}_Q Q(p, a) + c\sqrt{(\log N_p)/N_{p \rightarrow a}}$ 
11:     $s^{t+1}, M^{t+1}, o_i^t, r_i^t \leftarrow \text{Simulate}(s^t, M^t, a_i^t, C^t)$ 
12:     $N_p \leftarrow 1 + N_p$ 
13:     $N_{p \rightarrow a_i^t} \leftarrow 1 + N_{p \rightarrow a_i^t}$ 
14:     $p' \leftarrow p + (a_i^t, o_i^t)$ 
15:     $R \leftarrow r_i^t + \gamma \cdot \text{UpdateTree}(s^{t+1}, M^{t+1}, t+1, p')$ 
16:     $Q(p, a_i^t) \leftarrow Q(p, a_i^t) + R - Q(p, a_i^t)/N_{p \rightarrow a_i^t}$ 
17:     $return\ R$ 

1: procedure  $\text{ROLLOUT}(s^t, M^t, t)$ 
2:    $R \leftarrow 0, t' \leftarrow t$ 
3:   while  $t' < H$  do
4:      $C^{t'} \leftarrow \text{SampleConfiguration}(s^{t'}, M^{t'})$ 
5:      $a_i^{t'} \leftarrow \text{SampleAction}(A_i)$ 
6:      $s^{t'+1}, M^{t'+1}, o_i^{t'}, r_i^{t'} \leftarrow \text{Simulate}(s^{t'}, M^{t'}, a_i^{t'}, C^{t'})$ 
7:      $R \leftarrow R + \gamma^{t'-t'} \cdot r_i^{t'}, t' \leftarrow t' + 1$ 
8:    $return\ R$ 

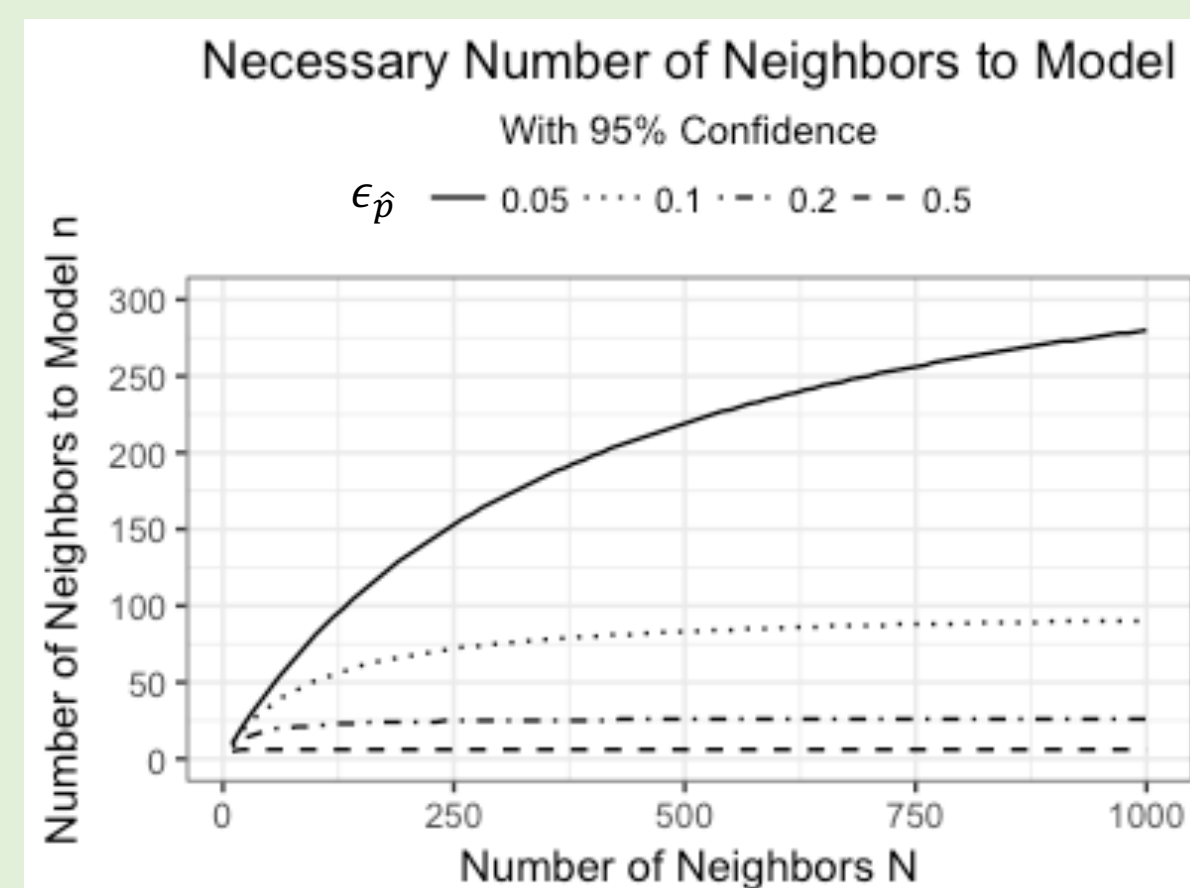
1: procedure  $\text{SAMPLECONFIGURATION}(s^t, M^t)$ 
2:    $C(a, \theta) \leftarrow 0, \hat{n}_{\pi(s^t)=a, \hat{N}_\theta(i)} \leftarrow 0 \quad \forall a, \theta$ 
3:   for  $M_{j, l-1} \in M^t$  do
4:      $a \sim \pi_{j, l-1}(s^t)$ 
5:      $\hat{n}_{\pi(s^t)=a, \hat{N}_{\theta_j}(i)} \leftarrow \hat{n}_{\pi(s^t)=a, \hat{N}_{\theta_j}(i)} + 1$ 
6:   for  $\theta \in \Theta$  do
7:     for  $a \in A$  do
8:        $\hat{p}_{a, N(i)} \leftarrow \hat{n}_{\pi(s^t)=a, \hat{N}_\theta(i)} / |\hat{N}_\theta(i)|$ 
9:     for  $j \in N_\theta(i)$  do
10:       $a \sim \text{Cat}(\hat{p}_{a_1, \hat{N}_\theta}, \hat{p}_{a_2, \hat{N}_\theta}, \dots, \hat{p}_{a_{|A|}, \hat{N}_\theta})$ 
11:       $C(a, \theta) \leftarrow C(a, \theta) + 1$ 
12:    $return\ C$ 

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Theoretical Results

Theorem 1 With confidence $1 - \alpha$, the *error* incurred by the subject agent in its estimate of the proportion $\hat{p}_{a, \hat{N}_\theta(i)}$ of its neighbors of frame θ that will perform action a is *bounded by the given* $\epsilon_{\hat{p}}$ so long as it models the following number of neighbors:

$$n_\theta = |\hat{N}_\theta(i)| \geq \frac{N \left(\frac{t_{n-1, \frac{\alpha}{2}}}{\epsilon_{\hat{p}}} \right)^2}{N - 1 + \left(\frac{t_{n-1, \frac{\alpha}{2}}}{\epsilon_{\hat{p}}} \right)^2}$$



Corollary 1 The *maximum error in the multinomial distribution* of the configuration of other agents' actions $P(C | s^t, M^t)$ is *bounded by*:

$$\epsilon_{P(C)} = |P^*(C | s^t, M^t) - P(C | s^t, M^t)|$$

$$< \frac{\prod_\theta |N_\theta(i)|!}{\prod_{\theta, a} C(a, \theta)!} \left[\prod_{\theta, a} (\hat{p}_{a, \theta} - \epsilon_{\hat{p}})^{C(a, \theta)} - \prod_{\theta, a} \hat{p}_{a, \theta}^{C(a, \theta)} \right]$$

when the subject agent models only n_θ neighbors (from Theorem 1) to achieve at most $\epsilon_{\hat{p}}$ error in its estimates of the action probabilities parameterizing the multinomial distribution.

Theorem 2 The *regret* of the subject agent from modeling only a subset of its neighbors is *bounded by*:

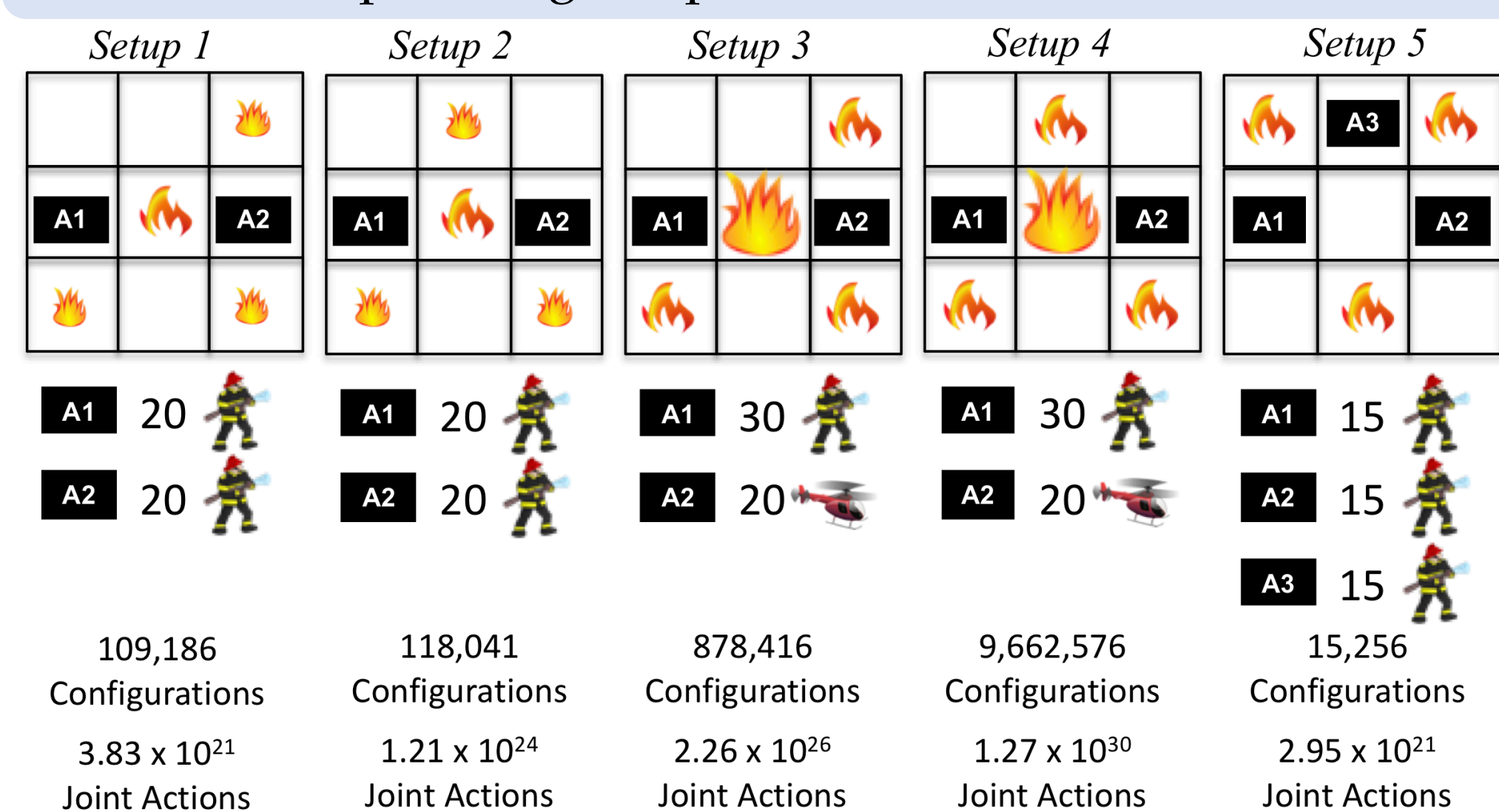
$$\|V_{i, k}^* - J_{i, k}\|_\infty \leq 2\epsilon_{P(C)} \cdot |C| \cdot R_{\max} \left[\gamma^{k-1} + \frac{1}{1-\gamma} \left(1 + 3\gamma \frac{|\Omega_i|}{1-\gamma} \right) \right]$$

which is *linear* in the error $\epsilon_{P(C)}$ in the agent's estimation of configuration likelihoods caused by modeling some neighbors only and *proportional to only $\sqrt{1/n_\theta}$ in the worst case* (due to the fact that $\epsilon_{P(C)}$ is at worst linear in $\epsilon_{\hat{p}}$ and $\epsilon_{\hat{p}}$ is proportional to $\sqrt{1/n_\theta}$)

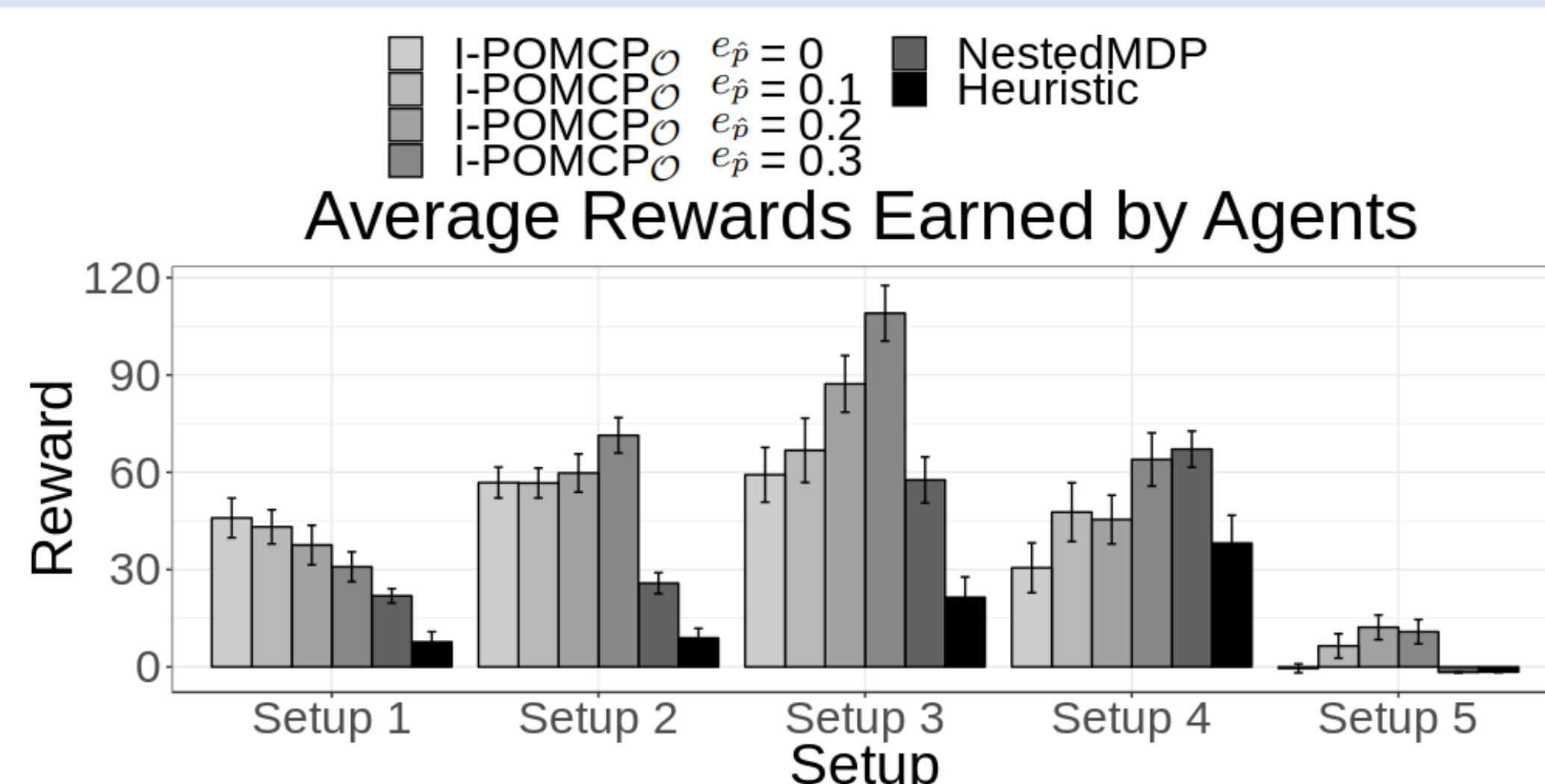
Experimental Results

Wildfire Problem: ground firefighter and helicopter agents with different capabilities cooperate to put out nearby fires.

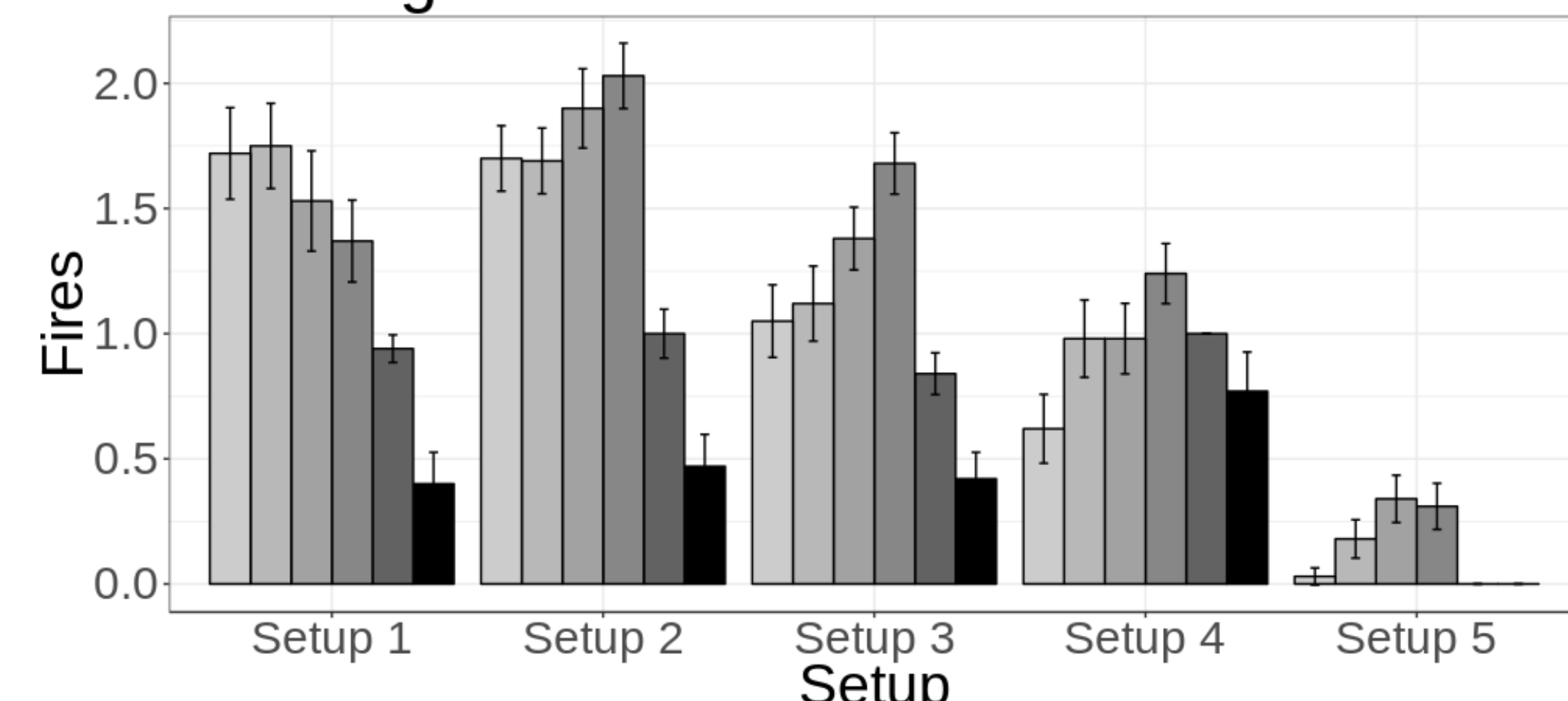
- Goal:** maximize rewards earned for putting out fires (and minimize costs for fires burning out)
- Agents can *run out of suppressant*, requiring them to temporarily leave the environment to recharge.
- Consider an order of magnitude more agents than prior studies on planning in open environments



Agent Reasoning Models: **Heuristic** randomly chooses active fires, **NestedMDP** is principled reasoning with value iteration at level 1, and **I-POMCP_O** is principled reasoning at level 2 with MCTS modeling n_θ neighbors from Theorem 1 based on $\epsilon_{\hat{p}}$ maximum error



Average Number of Fire Locations Put Out



- I-POMCP_O outperformed all baselines** (statistically significantly higher rewards in 4 of 5 setups) due to *better coordination* between agents by working together to put out fires in more locations
- In the more complicated Setups 2-4, *modeling fewer neighbors* n_θ due to higher allowable error $\epsilon_{\hat{p}}$ *led to improved performance* due to more sampled trajectories in the fixed time budget. This implies that the approximation error caused by modeling only some neighbors *was less than* the approximation error from sampling fewer trajectories in MCTS.