CS 275
Sample Final Exam

This is more or less the final exam from Fall 2018. I changed the wording on a few problems so it will make sense in Fall 2019, and I added a question on call/cc.

1. Write procedure (sizeOf L) which returns the number of atoms in general list L. For example (sizeOf '(a b (c d e) f (g)) h)) returns 8.
2. Write procedure (sort vec) where vec is a flat list of numbers. For example, (sort '(7 4 5 9 3)) returns (3 4 5 7 9).
3. Procedure (mfe lat) returns the most frequent element of the lat – the element that appears most often. If two elements tie for the largest multiplicity mfe can return either of them. For example (mfe ‘(a b a c d c b c d)) returns ‘c since there are 3 c’s, and 2 of each other letter, while (mfe ‘(a b a c d c b c a)) returns either ‘a or ‘c. Write (mfe lat).
4. The *depth* of a flat list is 1; the depth of a list containing a flat list is 2; the depth of a general list is 1 more than the greatest depth of any of its elements. For example, the depth of '(a (b) c (d (e (f g))) h) is 4 because the depth of (f g) is 1, the depth of (e (f g)) is 2, and the depth of (d (e (f g))) is 3. Use procedures *map* and *apply* to write function *(depth L)* which returns the depth of general list L.
5. **Explain in English what a closure is and why we need closures.** In particular, is there a property of the Scheme programming language that closures help us implement? You don’t need a full essay here; I can answer this question in 2 sentences.
6. In Lab 5 we made the following definitions for our environment datatypes:

```
(define empty-env (lambda () (list 'empty-env)))
(define extended-env (lambda (syms vals old-env)
                               (list 'extended-env syms vals old-env)))
```

We also made recognizers empty-env? and extended-env? and for the extended-env type we made getters syms, vals, and old-env.

Using these tools, write procedure (lookup env symbol) that returns the value bound to symbol in the given environment, or the value ‘oops if symbol is not bound in the environment.
Here are 5 terms commonly used when we talk about programming languages. Explain (1 sentence is sufficient; use more if you must) **what each of them means**:

a. call-by-value

b. call-by-reference

c. call-by-name

d. static binding

e. dynamic binding
8. In class we produced the stream Primes$ of prime numbers; you don’t need to reproduce this. **Use this stream Primes$ to produce the stream TwinPrimes$** that consists of pairs of primes that differ by 2. The first few elements of TwinPrimes$ are (3 5) (5 7) (11 13) (17 19) and (29 31).
9. Let’s say that a “lop” is a list of pairs, where the first element is a symbol and the second element is a number, such as ((a 5) (b 3)). Write a continuation-passing style function (increment-k sym amount lop k) that increments the pair of lop whose first element is sym by the given amount. If there is no such pair, the pair (sym amount) is added to the list. k, of course, is the current continuation. For example

```
(increment-k 'b 3 '((a 4) (b 2) (c 5)) (lambda (x) x)) returns ((a 4) (b 5) (c 5))
```

while

```
(increment-k 'd 3 '((a 4) (b 2) (c 5)) (lambda (x) x)) returns '((a 4) (b 2) (c 5) (d 3))
```

You can assume that only one pair in a lop will start with any given symbol.
10. What does this function return if you evaluate
   (f '(3 2 1 0 4 3 2 1 0))
   (define f
     (lambda (lat)
       (call/cc (lambda (k)
         (let ((g (lambda (y)
               (if (= 0 y)
                 (k 5)
                 (* y y)))
         (cond
           [(null? lat) 0]
           [else (+ (g (car lat)) (f (cdr lat)))]))))))

